



UNIVERSITÀ
DI TORINO



DBMSS

Dipartimento di Biotecnologie
Molecolari e Scienze per la Salute

Innovative
methodologies and
design of didactic
activities

Marina Marchisio

University of Turin (Italy)

With the patronage of



Innovative methodologies

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Adaptive Teaching

3

Multicultural
classrooms

International
mobility

Learning
diseases

“to apply different instructional strategies to different groups of learners so the natural diversity prevailing in the classroom does not prevent any learner from achieving success”

(Borich, 2011)

Different
learning styles

Individual
attitudes and
inclinations

Common
learning
objectives

Formative assessment

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“Practice in a classroom is formative to the extent that evidence about student achievement is elicited, interpreted, and used by teachers, learners, or their peers, to make decisions about the next steps in instruction that are likely to be better, or better founded, than the decisions they would have taken in the absence of the evidence that was elicited.”

(Black & Wiliam, 2009)

Strategies of formative assessment

clarifying and sharing learning intentions and **criteria for success**

engineering **learning tasks** that elicit evidence of student understanding

providing **feedback** that moves learners forward

activating students as instructional resources

activating students as the **owners of their own learning**



“information provided by an agent (e.g., teacher, peer, book, parent, self, experience) regarding aspects of one’s performance or understanding”

(Hattie & Timperley, 2007)

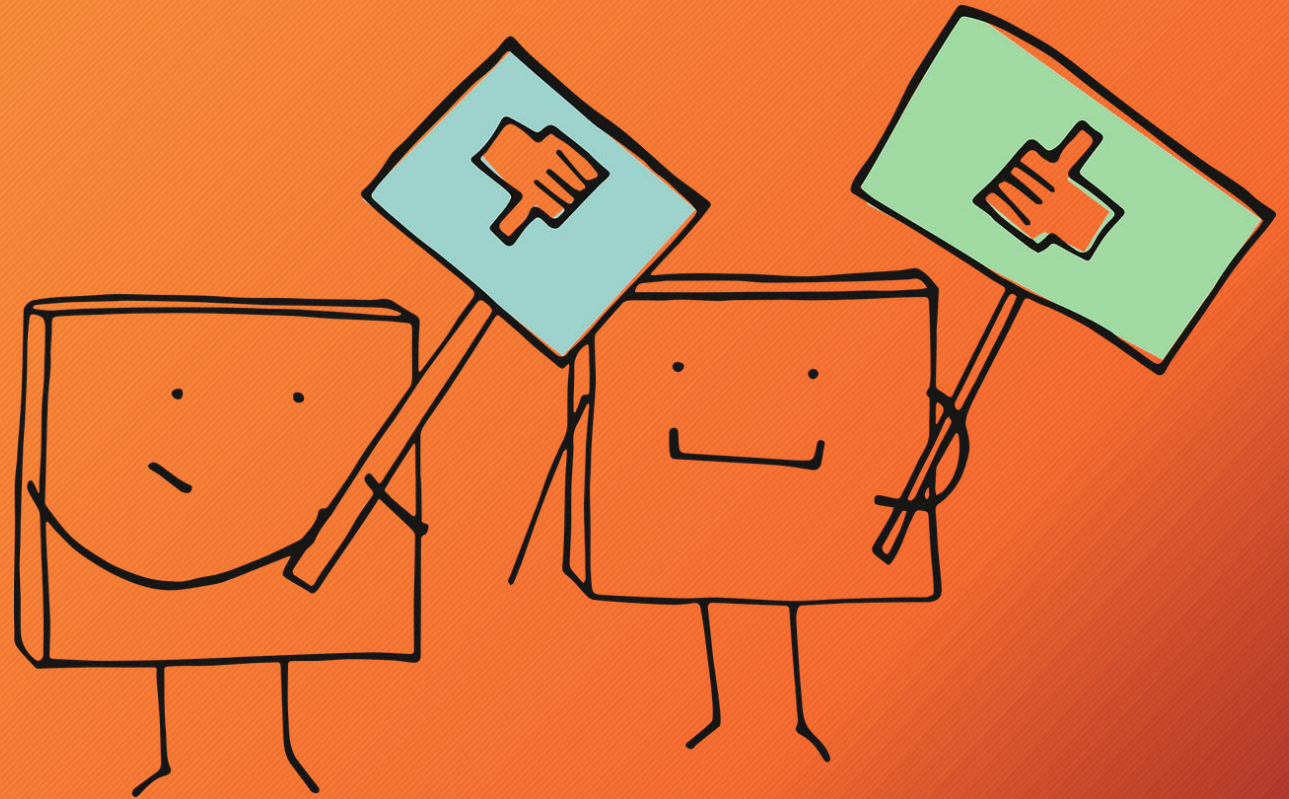
Feedback can work at 4 levels:

task level

process level

self-regulation level

self-level



Self-regulated learning

“self-regulated learning is an active constructive process whereby learners set goals for their learning and monitor, regulate, and control their cognition, motivation and behaviour, guided and constrained by their goals and the contextual features of the environment”

(Pintrich & Zusho, 2002)

Good feedback practice to enhance self-regulation

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helps clarify what **good performance** is

facilitates the development of **self-assessment**

delivers **high quality information** to students about their learning

encourages teacher and peer **dialogue** around learning

encourages **positive behaviours** and motivation

provides **opportunities to close the gap** between current and desired performance

provides **information to teachers** that can be used to help shape the teaching

Problem Posing in Mathematics

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Context

Real
Rich
Linked to
everyday life



Situation

Challenger
Coherent
Clear
Understandable
With more
possible
interpretations



Request

Contextualized
Adequate
difficulty
More solution
strategies
Requires math
skills



Problem

Multiple
resolutions
possible
It suggests
meaningful
reflection
Generalization
of the
resolution

Problem solving in Mathematics

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"The term "problem solving" refers to all mathematical tasks that have the ability to provide intellectual challenges to improve students' understanding and development of mathematical concepts, especially in dynamic real-world situations."

(National Council of Teachers of Mathematics, 2000)

Problem Solving

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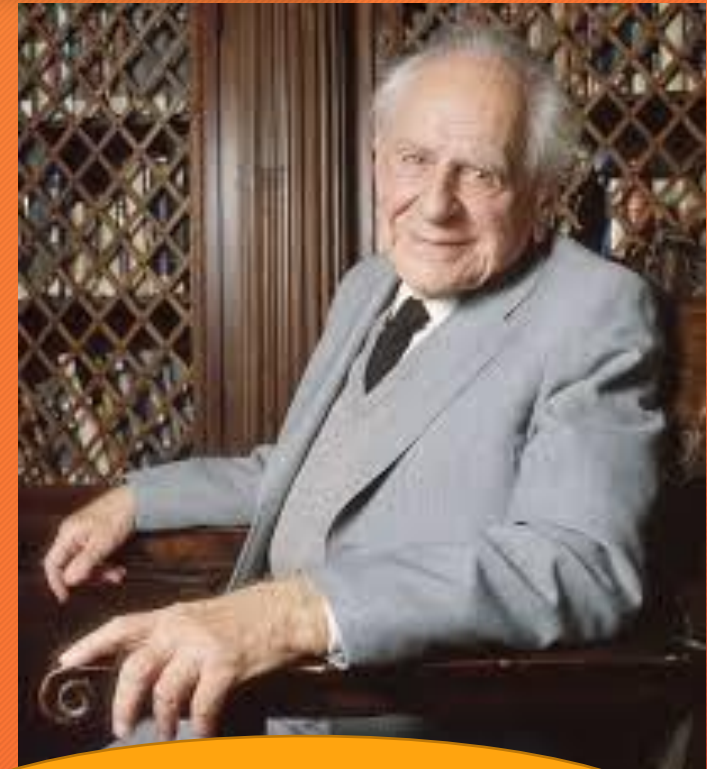
To learn new ideas, new approaches

To work in team

To apply knowledge in daily life

To face changes

To model a problem situation



All life is Problem Solving (Karl Popper)

Problem Solving

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Comparison

- with situations contextualized

Invention

- of new procedures thinking outside the conventional schemes

Creation

- of solutions with an original contribution, designing a strategy

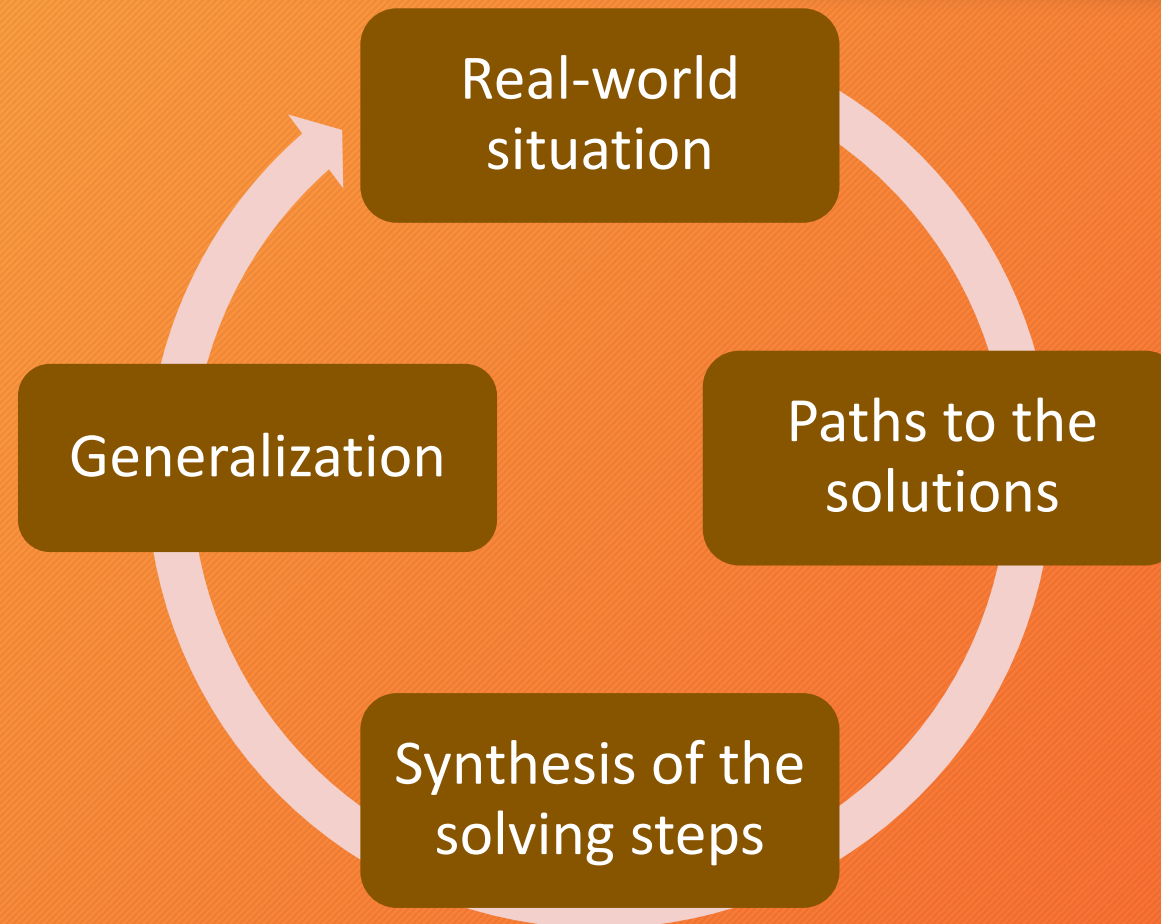
Description

- argumentation of the solution process using different representations

(Samo et al., 2017)

The problem solving process

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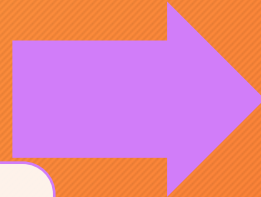
Mathematical Modelling

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The process of translating between the real world and Mathematics in both directions, where reality means the “rest of the world” outside Mathematics, including nature, society, everyday life, and other scientific disciplines

Models

- **representations that can describe and explain the phenomena of reality**



Using models

- **to obtain predictions on the progress of experiments, mechanisms and processes**

Mathematical Modelling

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Helping students to better understand the world

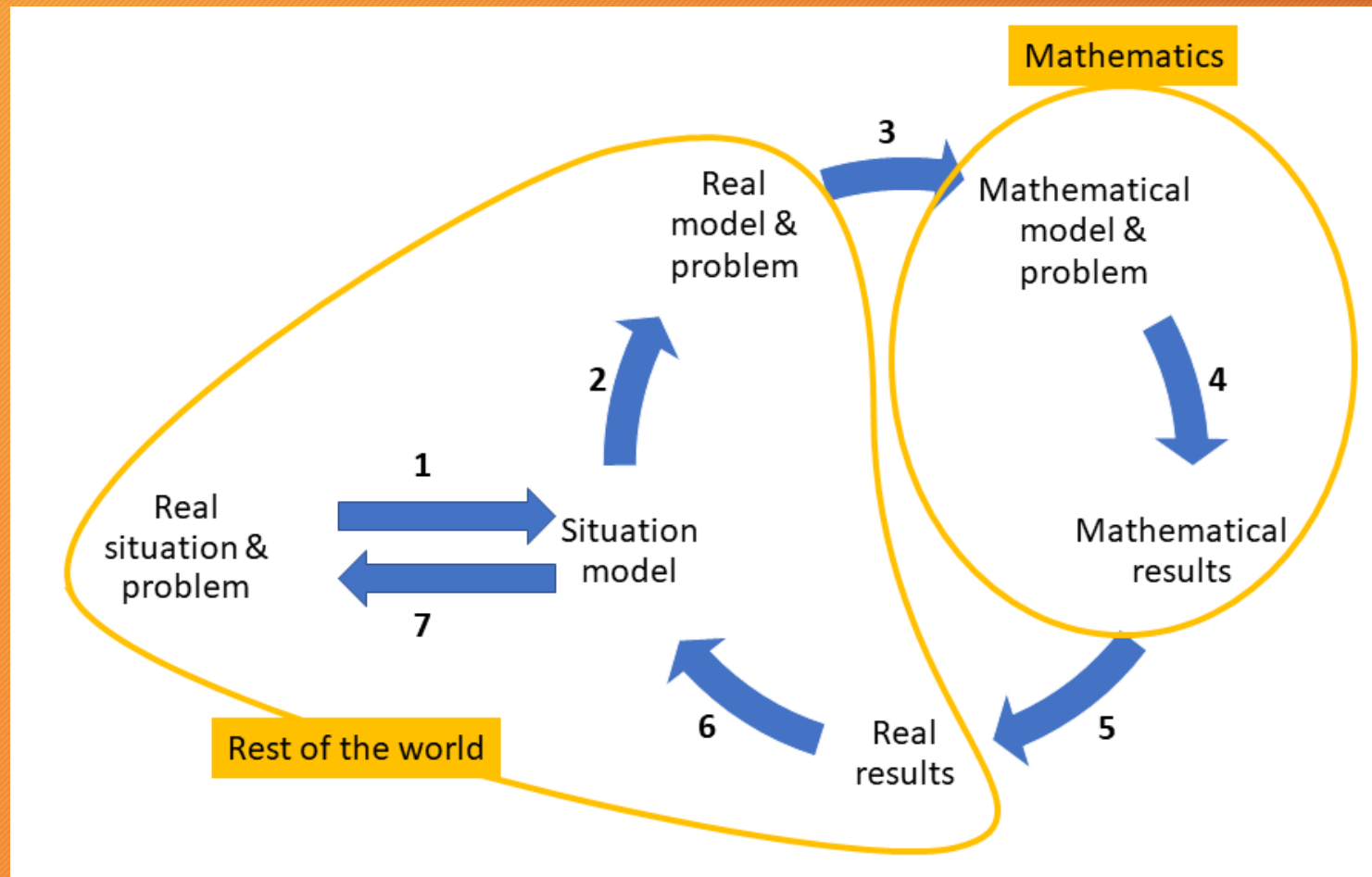
Supporting Mathematics learning (motivation, concept formation, comprehension, retaining)

Contributing to develop various **mathematical competencies** and appropriate attitudes

Contributing to an adequate **picture of Mathematics**

Seven-step model of the “modelling cycle” for research and teaching purposes

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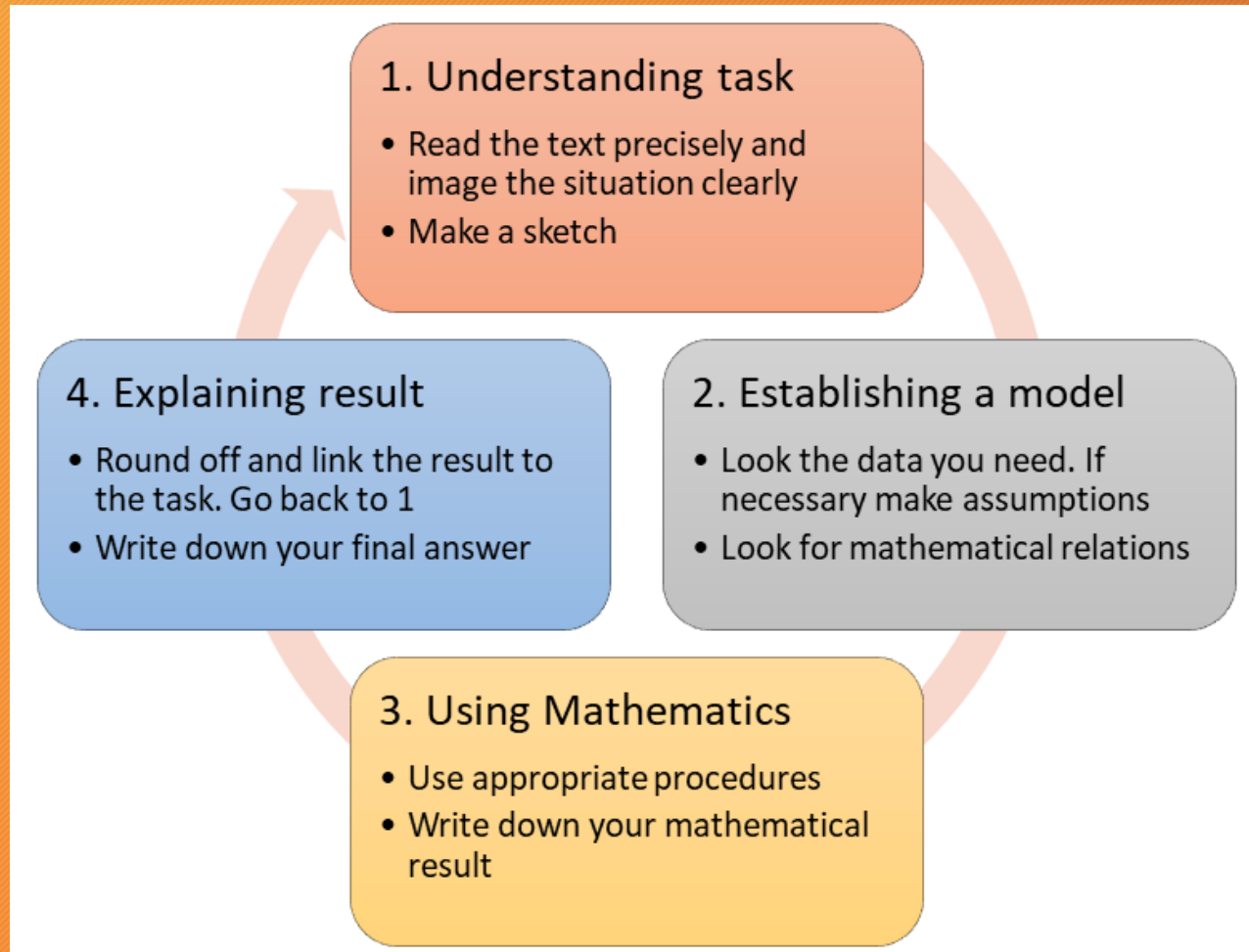


Modelling is inseparably linked with other mathematical competencies

(Blum & Leiß, 2007)

Four-step model of the “modelling cycle” for student’s activities

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“modelling competency” is the ability to construct models by carrying out all the steps and to analyse or compare given models

Collaborative Learning

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A didactic methodology to make two or more people learn together

Educational approach that the group uses to improve learning

Groups of two or more people working together to solve problems, complete goals, and learn new concepts



Collaborative learning keywords

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Group

- Leadership
- Coordination
- Peer
- Responsibility

Cooperation

- Competition
- Listening
- Interaction
- Instruments

Competences

- Express ideas
- Defending ideas
- Public Speaking
- Soft skills

Active learners

- Feedback
- Self-esteem
- Self evaluation
- Integration

To prepare students for real situations of social life and the world of work

Collaborative learning for professional development

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Collaboration
=
key factor for professional
development



- Teachers learn through collaborating with others
- Articulating and sharing ideas
- Finding solutions to the challenges posed within their context

(J. Deppeler, 2007)

Learning by doing

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In the context of scientific disciplines, the **experimental dimension** must always be kept in mind

It is appropriate to identify some particularly significant **experimental activities** to be carried out in the laboratory, in the classroom or online, to be privileged over purely theoretical and/or mnemonic activities

A workshop activity can be understood as a **teaching-learning environment** that can be compared to the Renaissance workshop, where one learned by doing and seeing done, communicating with classmates as well as by imitation of the expert

Activity

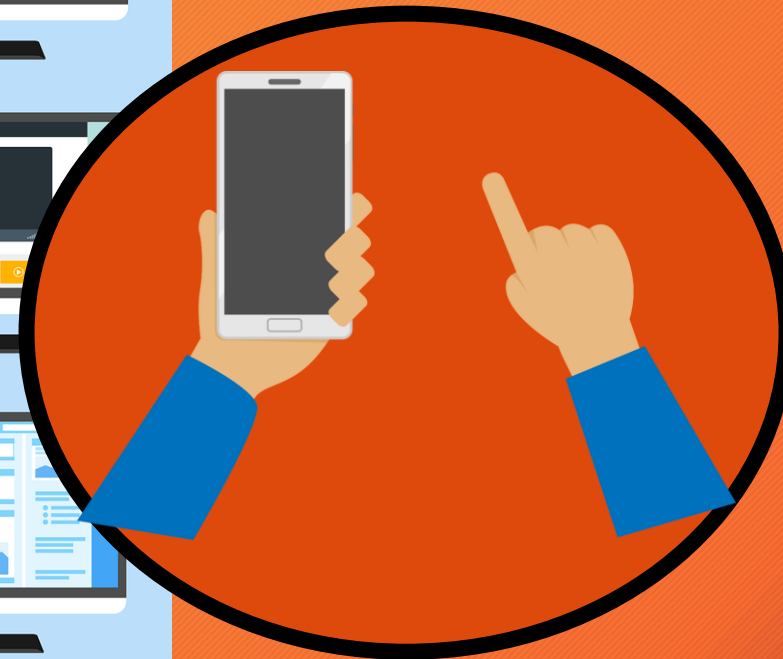
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- As a student, have you ever participated in activities in which one of these methodologies was used?
- What is your opinion on these methodologies?

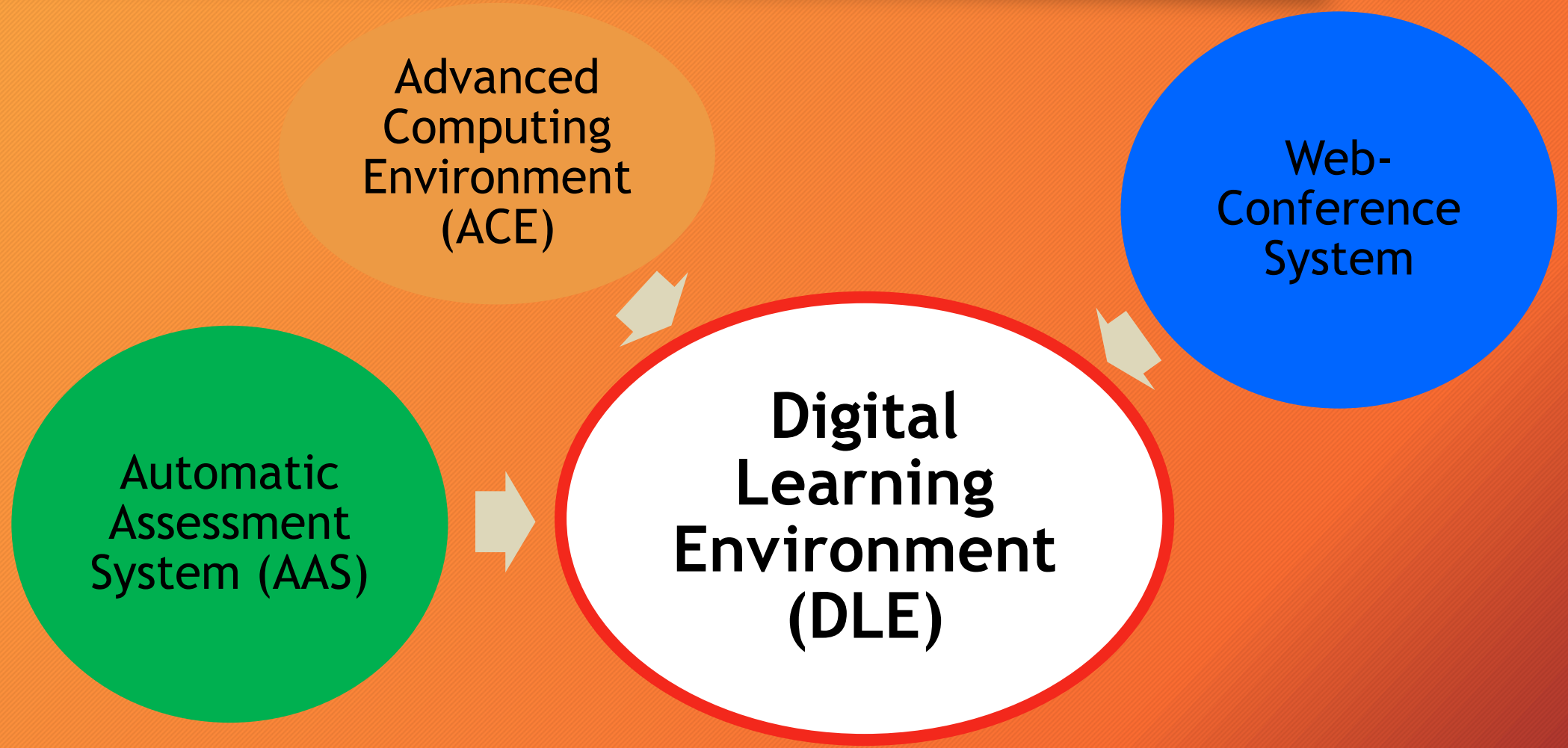
Technologies can support these methodologies

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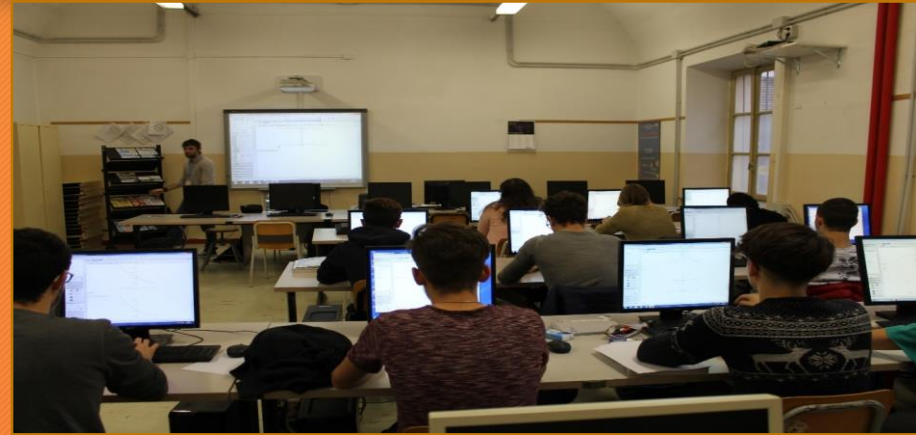
Technologies used in adaptive strategies

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DLE

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(Fissore, Marchisio & Rabellino, 2020)

Adaptive strategies in DLE

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Continuous Support

Tracking progresses and activities

Teachers can find out interests, difficulties of students and use information to create contexts

Collaborative learning, peer evaluation

Interactivity and interaction

Suitable material for Dyslexic



- Synchronous and asynchronous discussion
- Integrated gradebook
- Questionnaires and user details
- Workshop
- Integration with the tools for computing and assessment
- EasyReading, high-readability font

Adaptive strategies supported by AAS

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Formative assessment

Time optimization

Open Math answers

Algorithm based questions

Find the value of k for which $(1+k)x - 4ky - 2 = 0$ is a line parallel to the x-axis.

k=

Write the equation of the sheaf of lines which corresponds to the value of k that you have found.

Then, click on the **P** icon to visualize the graphic of the line and to check that it belongs to the sheaf.

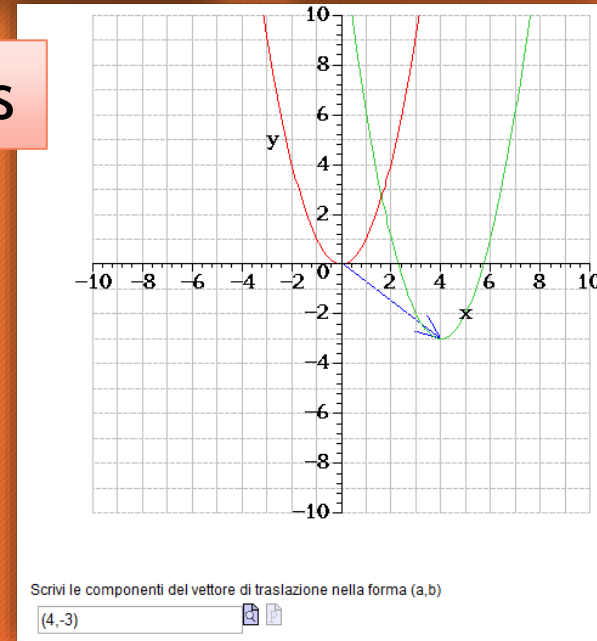
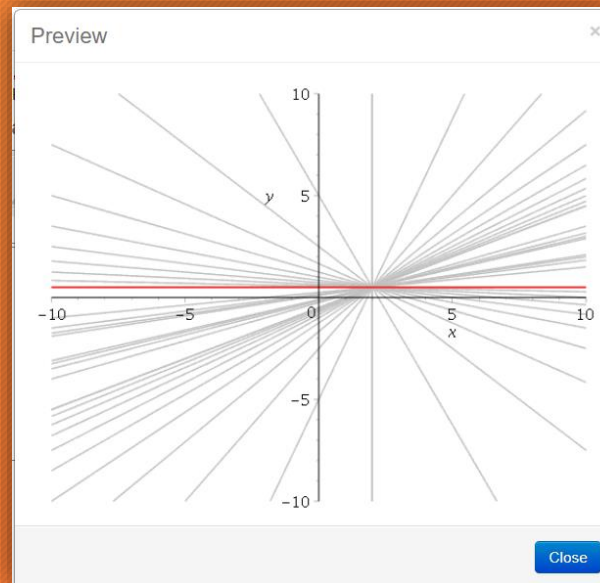
Equation Editor

Equation Editor interface showing a toolbar with mathematical symbols like a^b , $\sin(a)$, $\frac{\partial}{\partial x} f$, a grid icon, ∞ , α , Ω , a refresh icon, and a Help button. The input field contains the equation $y = \frac{1}{2}$.

Grade

Refresh

Close



Adaptivity

Immediate feedback

Ten good reasons to adopte the AAS

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STUDENTS

1. Availability
2. Immediate feedback
3. Adaptivity
4. Learning from mistakes
5. Respect of rules

TEACHERS

6. Feedback
7. Change of role
8. Teacher training
9. Saving resourses
10. Repository of questions

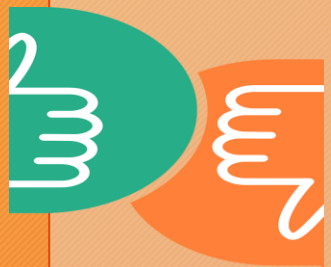


Standardized/summative assessment

- Teachers can automatically evaluate, collect and analyze students' responses



In Italy INVALSI tests (Mathematics, English and Italian disciplines)
<https://INVALSI-areaprove.cineca.it/>



Formative assessment

- Students can be trained in self-assessment to better prepare themselves



Model for automatic formative assessment through the use of an AAS

Our model of automatic formative assessment

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Availability

Algorithm-based questions and answers

Open answers

Immediate feedback

Interactive feedback

Contextualization

✘ An ice-creamer needs to cover the inner surface of the cones with black cherry sauce.
Given that the inner height of a medium cone measured 11 cm the inner diameter is 5.6 cm long, calculate the measure of the inner surface that should be covered with black cherry sauce.
Approximate the result to the nearest integer.

Result = cm^2

✔ We need to compute the area of the inner surface of the cone, given that its measures are the following:

- heigh: cm ✔
Correct response: 11 cm
- radius: cm ✔
Correct response: 2.8 cm

✔ To compute the area of the lateral surface we need to know how much the apothem is long.
You can compute its measure by the formula: $a = \sqrt{h^2 + r^2}$
Round the result to the second digit.

$a =$ cm ✔
Correct response: 11.35±0.01 cm

Now we can compute the area of the lateral surface by the formula $S_l = r \cdot a \cdot \pi$.

$S_l =$

Round the result to the nearest integer.

Attempt 1 of 1

(Barana, Fissore & Marchisio, 2020)

Our model of automatic formative assessment

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Availability

Algorithm-based questions and answers

Open answers

Immediate feedback

Interactive feedback

Contextualization

Test with
automatic
assessment

Multiple
attempts

Encourage
positive
motivational
beliefs and self-
esteem

Our model of automatic formative assessment

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Availability

Algorithm-based questions and answers

Open answers

Immediate feedback

Interactive feedback

Contextualization

Variable parameters and formulas

Focus on processes and not on results

In the case of multiple attempts, the feedback information can be used to bridge the gap between current and desired performance

Our model of automatic formative assessment

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Availability

Algorithm-based questions and answers

Open answers

Immediate feedback

Interactive feedback

Contextualization

The multiple choice answer mode is not used exclusively

The use of different registers in the answers is required: words, numbers, symbols, tables, graphics, diagrams

Our model of automatic formative assessment

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Availability

Results shown while students are focused on the activity

Algorithm-based questions and answers

Open answers

Immediate feedback

No more than 5 questions per assignment

Interactive feedback

Contextualization

Facilitates the development of self-assessment

Our model of automatic formative assessment

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Availability

Algorithm-based questions and answers

Open answers

Immediate feedback

Interactive feedback

Contextualization

Step-by-step guided resolution

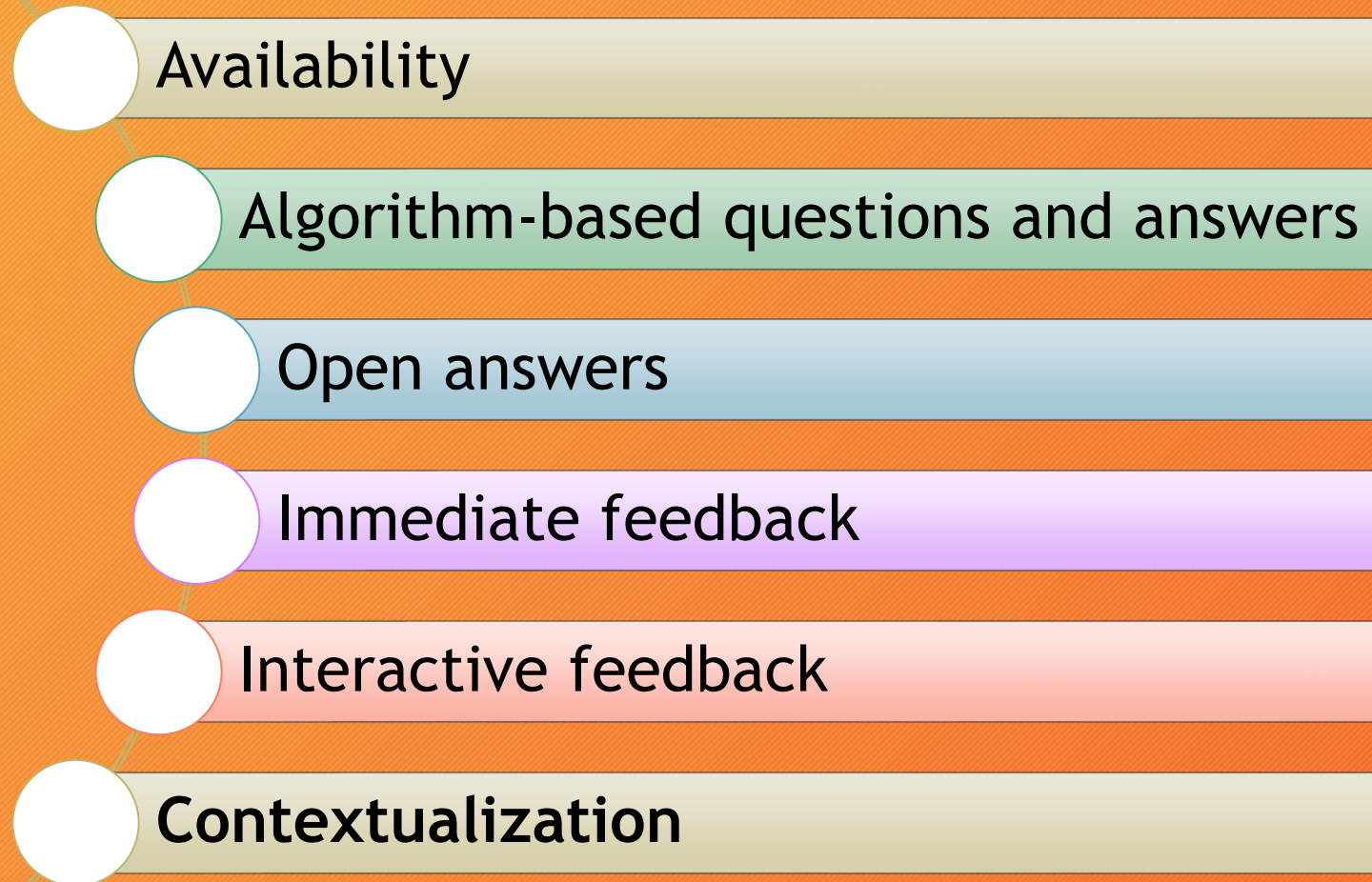
Provides interactive standards

It helps to clarify what the good performance is

Provides high quality information: background and process that allows students to solve the problem

Our model of automatic formative assessment

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Real
context

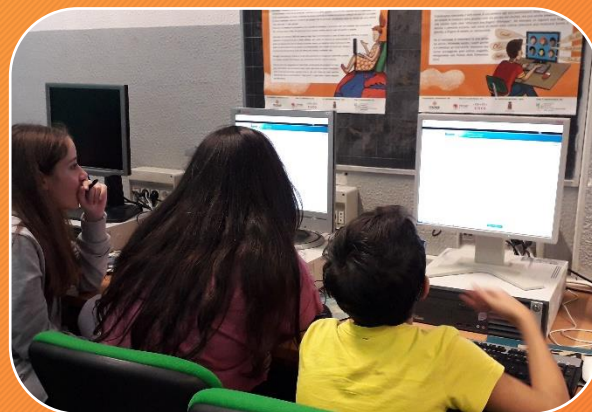
It contributes to
the creation of
meanings and to
a deeper
understanding

Organize work with the AAS with students

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In the classroom
with BYOD
modality



In the laboratory



In class with pen
and paper using
the IWB

formule

- Fogli elettronici e funzioni - 1
- Fogli elettronici e funzioni - 2
- Operazioni con numeri e lettere
- Giochiamo con le frazioni
- Vero o falso?

Online

DLE for STEM: ACE

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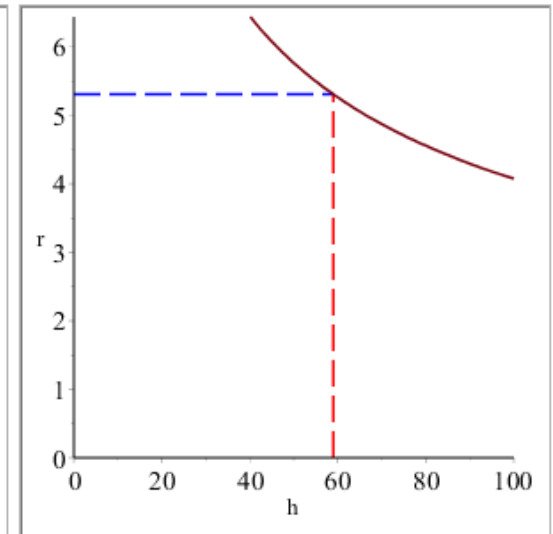
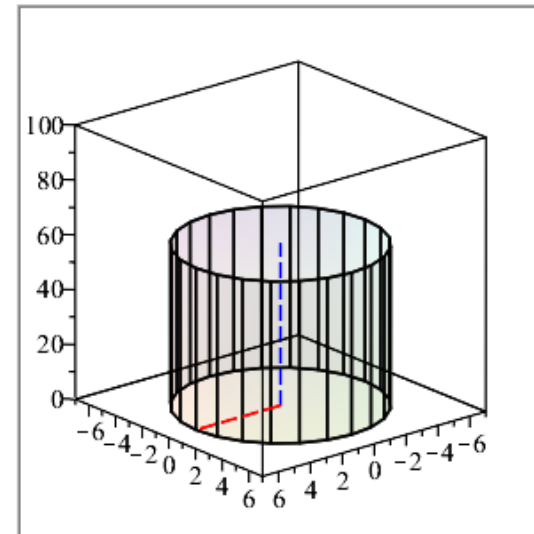
- ✓ Numeric computations
- ✓ Symbolic calculus
- ✓ Graphical representations, static and animated, in 2 and 3 dimensions
- ✓ Procedures in a simple programming language
- ✓ Interactive components to visualize how a results change when the input parameters are changed
- ✓ Connecting all the **different representation registers** in a single worksheet

Tool to enhance teaching and learning of STEM

Observe how the form of the cylinder of given volume changes depending on its height.

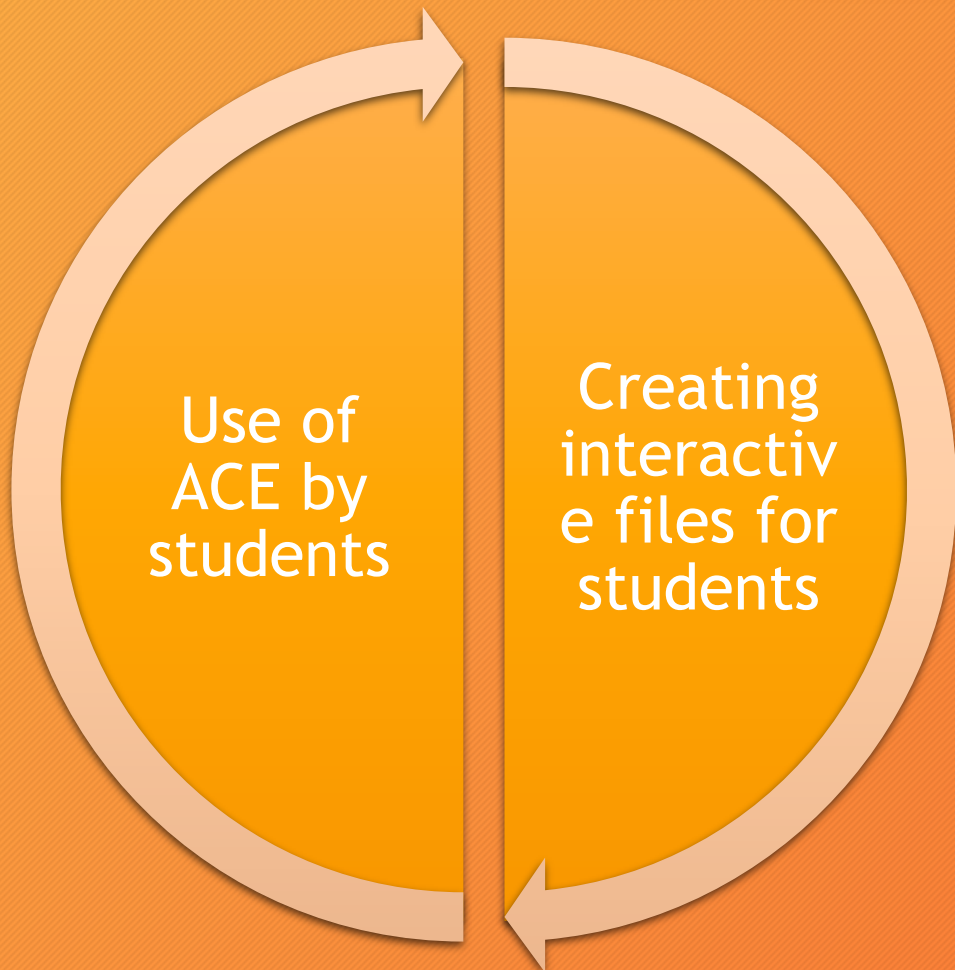
$h =$

$$r = \sqrt{\left(\frac{5225}{\pi \cdot 59}\right)}$$



DLE integrated with the ACE

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Thanks to the integrated platform, files created with ACE can be uploaded to the platform and viewed even without having installed the software, maintaining interactivity

- For recovery
- For strengthening
- To develop problem solving skills
- To study, review or deepen theoretical concepts

The use of an ACE

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Extends ways of reasoning on mathematical tasks

Enhances exploration of multiple representational forms
(e.g., numerical, symbolic, graphic)

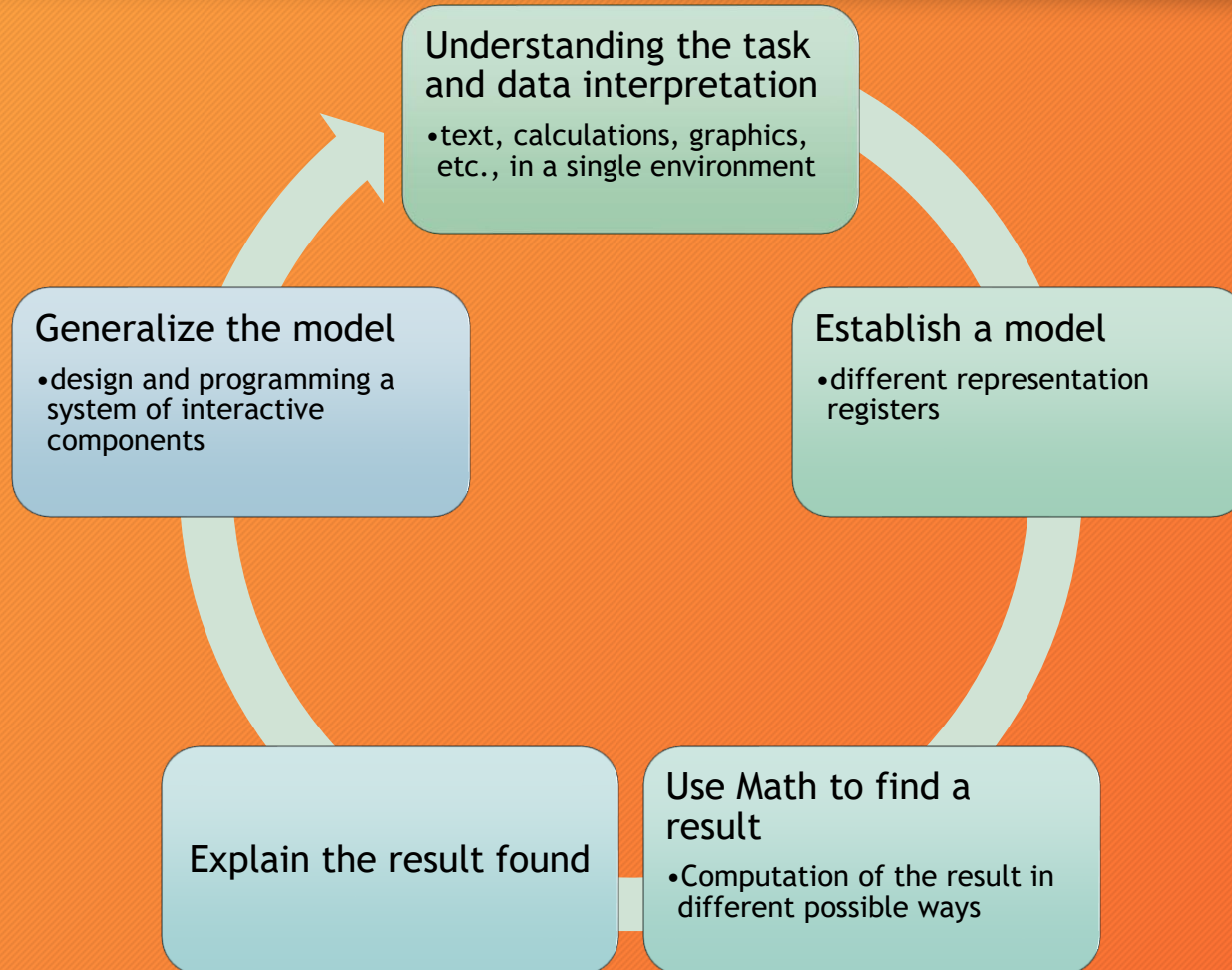
Allows to represent and explore dynamically mathematical tasks

Allows to generalize the solving process of a problem

Allows to create interactive files in which the user interacts with the software

Our "Solution Plan" for modelling activities with an ACE

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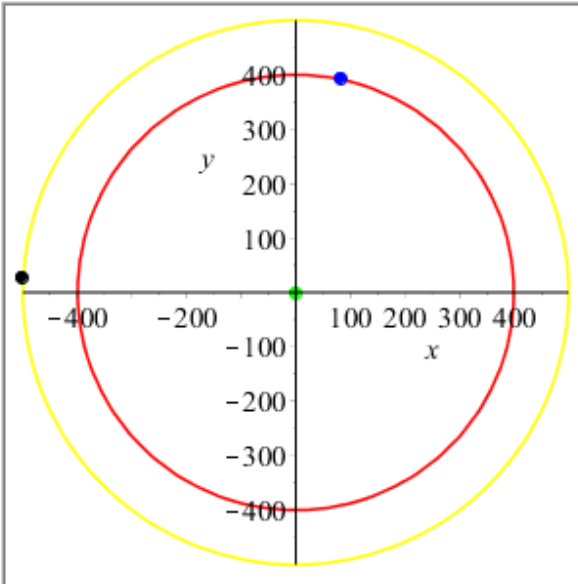
Example of interactive material

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Satellite angle 1 (in degrees) Satellite angle 2 (in degrees)

Satellite angle 1 converted into radians: Satellite angle 2 converted into radians:

View perpendicular to the plane of the 2 orbits:



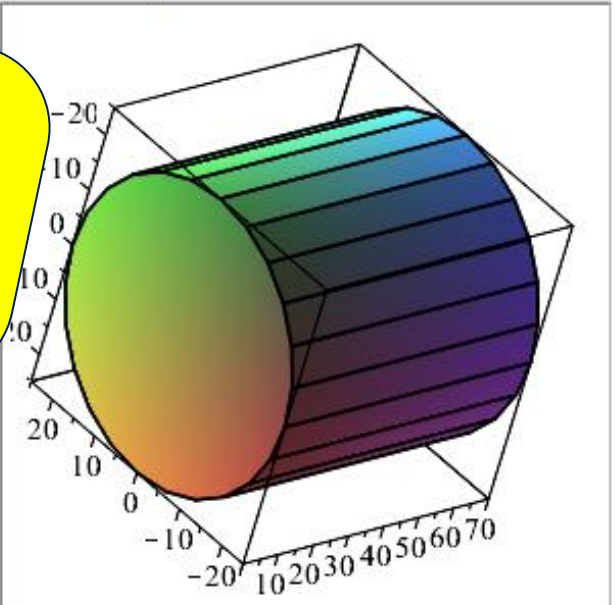
Distance as the crow flies between the 2 satellites [km] Conclusion:

As the slider cursor changes, the graphs change accordingly

Radius R: mm

Length L: mm

3D drawing of the circular section beam:



Example of interactive material

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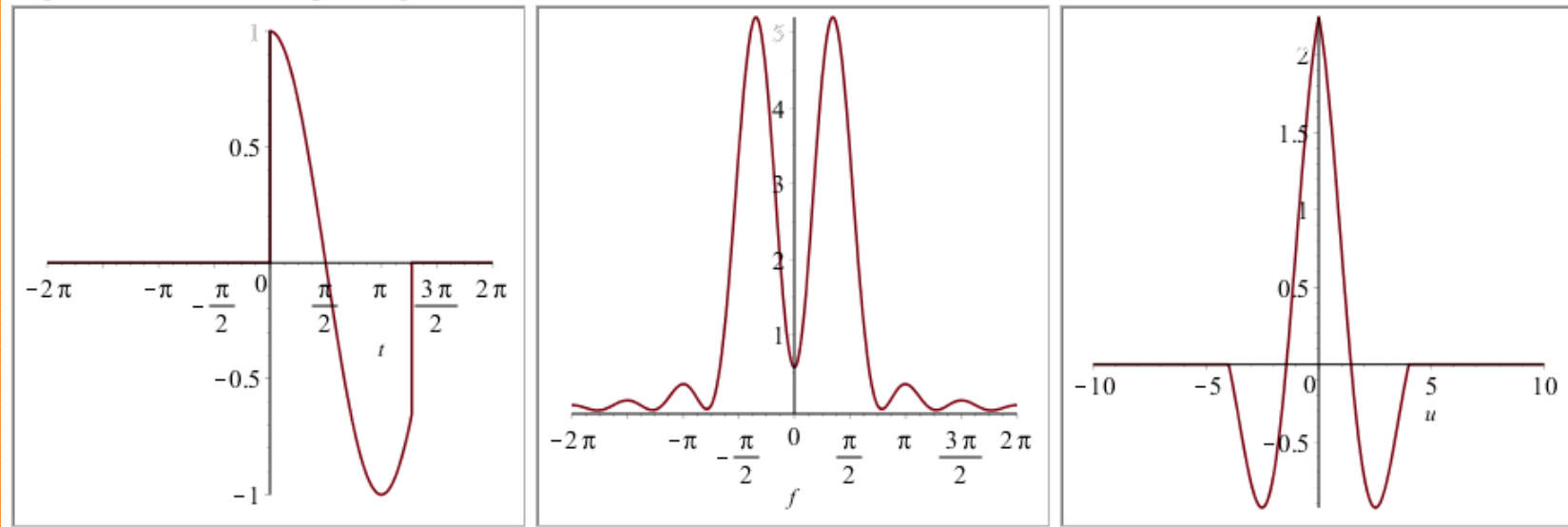
Study of finite energy signals, their spectrum and autocorrelation

Define the support:

a = b =

Define the (real) function on [a, b]:

Graphs of the function, its amplitude spectrum and its autocorrelation:



1. INPUT DATA

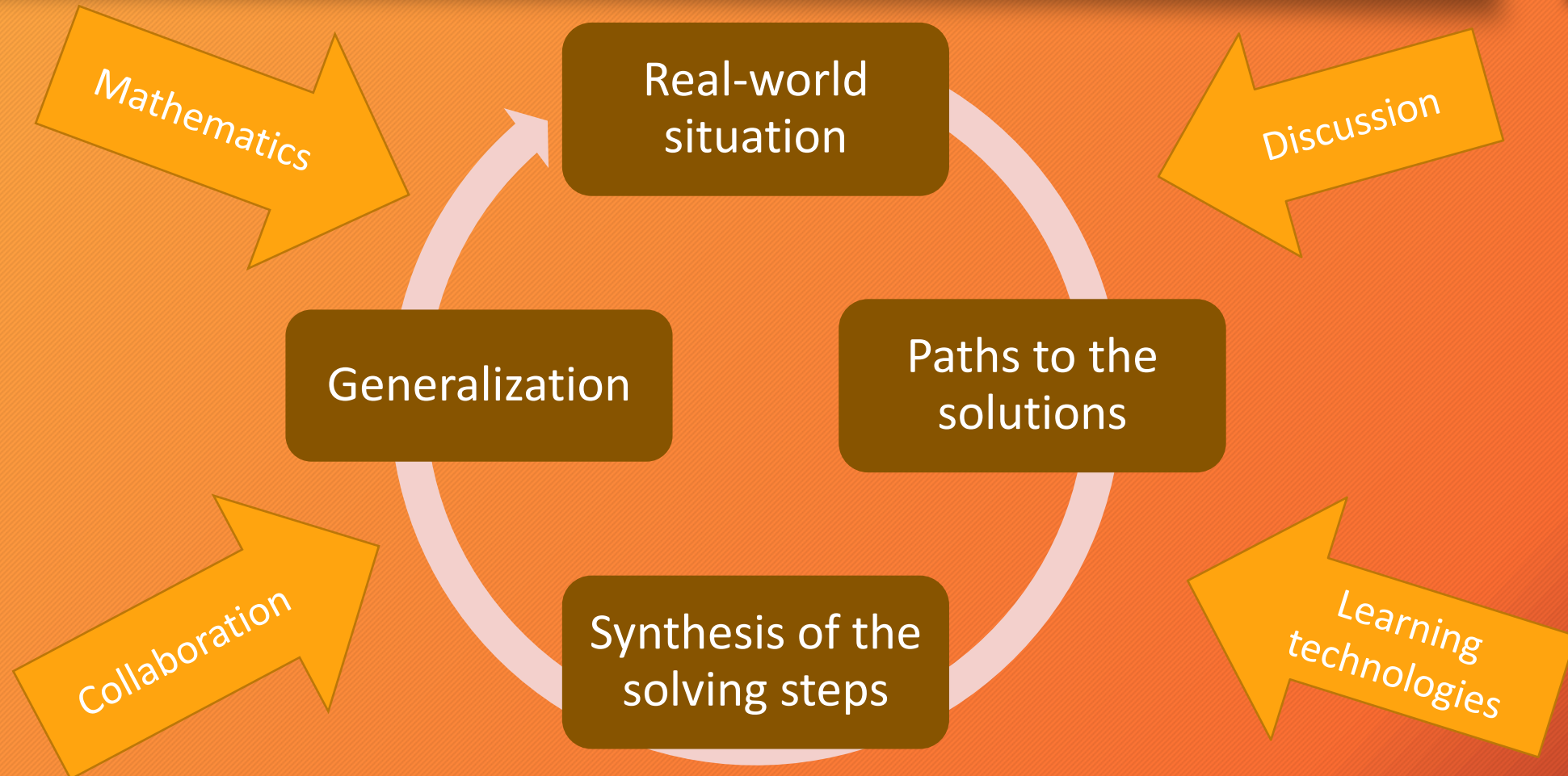
2. CLICK THE BUTTON

3. OUTPUT DATA

**Study of
signals**

Adaptive strategies in Problem Solving

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Adaptive strategies in Problem Solving

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- Engaging starting points, adapted to students' interests
- Motivational lever
- Facilitate comprehension of theory
- Clarify usefulness of Mathematics

SUN'S HEIGHT ABOVE THE HORIZON

Problem

At a certain time of the day the shadow of a building turns out to be shorter than his actual height. How much high can the Sun be on the horizon?

Resolution

Clearly, when we talk about the "height of the Sun," we do not mean an actual height measured in meters. We rather mean the inclination of the Sun's rays with respect to the surface of the Earth.

Let's model the problem by indicating the height of the building with the letter h ; we denote by x the angle corresponding to the inclination of the solar rays with respect to the surface. By finding the inclination angle x , corresponding to the angle \widehat{CAB} of the figure below, we would know the height of the Sun on the horizon.

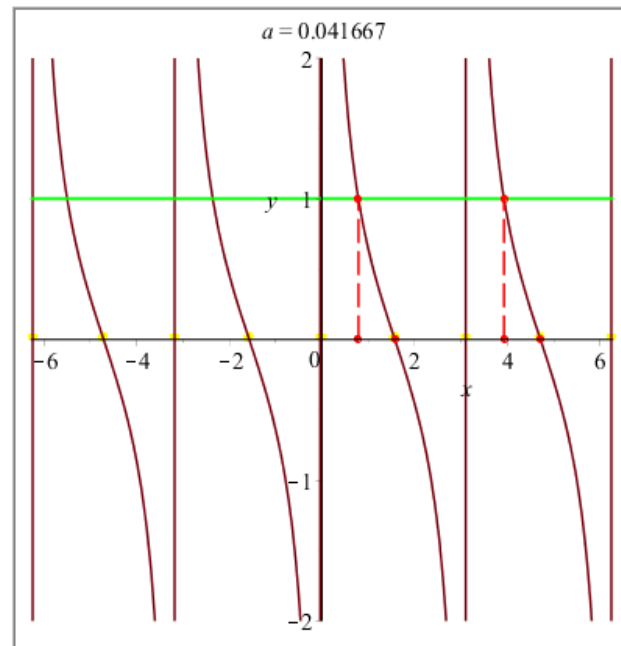
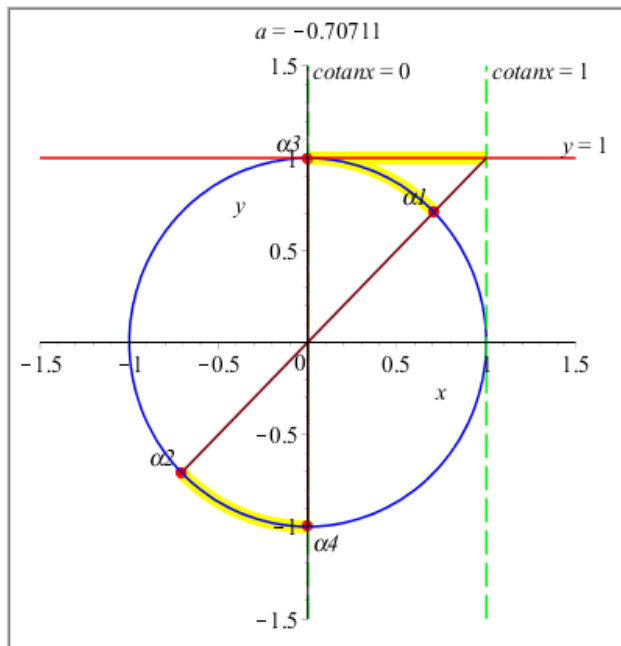
Adaptive strategies supported by ACE

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The solution to the system

The solution to the system is the following: press the button below and then activate the two animations.

Click to view the graphs



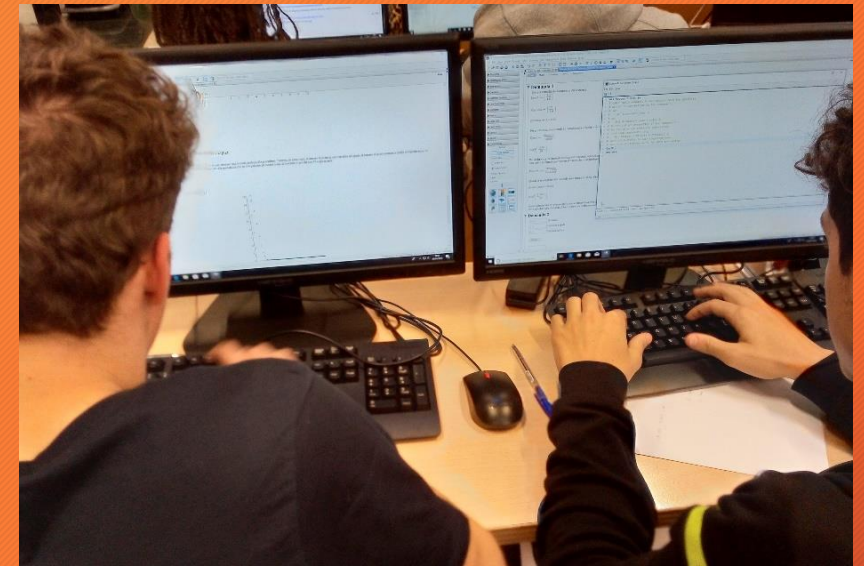
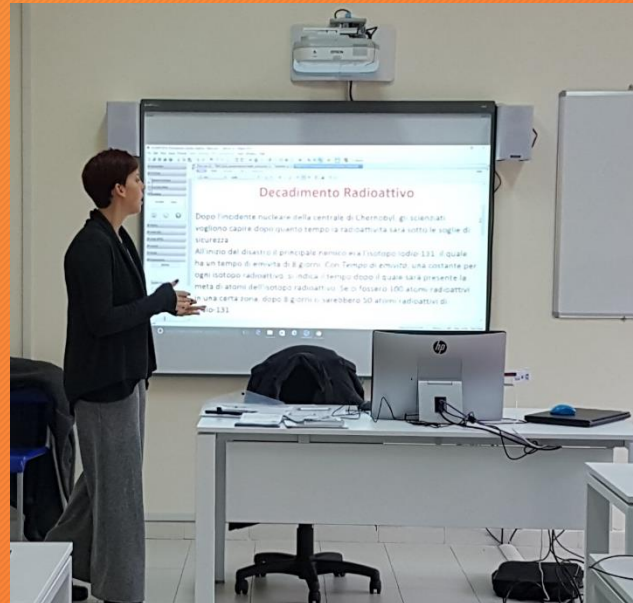
Reset

The solution is $\frac{\pi}{4} < x < \frac{\pi}{2} \vee \frac{5}{4}\pi < x < \frac{3}{2}\pi$

- Exploration of possible solutions
- Interactivity
- Different ways of representation
- Feedback from automatic computations
- Autonomous study, guided by the tutor

Problem solving activities with students within the DLE

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Online math educational software

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Use of cloud systems and free software for sharing resources (including interactive)

- Geogebra cloud
- Wolfram|Alpha (<http://www.quickmath.com/>)
- Maple Learn (<https://learn.maplesoft.com/>)

Collaborative Learning in the DLE

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Community
of teachers



Community
of students

Community
class

Collaborative Learning in the DLE

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Not just
online



DLE for asynchronous collaboration

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It amplifies peer support

It supports the dynamics of interaction and participation within a group

It allows you to expand the space for interactions, giving you more possibilities for expression

Es: Forum

Activity

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- What characteristics do the presented methodologies have in common?

Students are Protagonists!

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Awareness

Repeat the
reasoning

Work
independently

Management
of time

Self
organization

Actively try
and explore

Design of didactic activities

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Didactic planning index

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1. Regulations

2. Objectives /
Prerequisites

3.
Methodologies

4. Type of
activities and
timing

5. Technologies

6. Poor and
interactive
materials

7. Multi- and
interdisciplinary

8. Inclusion

9. Evaluation

10.
Metariflexion

1. Regulations

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The planned activity must always be framed within the existing legislation



Ministero dell'istruzione, dell'università e della ricerca

Schema di regolamento recante "Indicazioni nazionali riguardanti gli obiettivi specifici di apprendimento concernenti le attività e gli insegnamenti compresi nei piani degli studi previsti per i percorsi liceali di cui all'articolo 10, comma 3, del decreto del Presidente della Repubblica 15 marzo 2010, n. 89, in relazione all'articolo 2, commi 1 e 3, del medesimo regolamento."

Example: "Italian national guidelines regarding the specific learning objectives concerning the activities and teachings included in the study plans for high school pathways" (2010)



2. Objectives/Prerequisites

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Topic

Specific topic that is covered in the activity

Class

Class that students attend

Type of institution

Specify the type of institution

Period

In what period of the school year?

Context

- Context in which the problem or proposed exercise is inserted

Didactic objectives

- What training objectives do you want to achieve through this activity?

Prerequisites

- What do participants need to know in order to perform the activity in the best possible way?

Estimated time

- Estimated time for carrying out the activity with the students

2. Objectives/Prerequisites

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What knowledge
do I want you to
learn?

What skills do
I want to
acquire?

What skills do I want to
develop
(disciplinary/transversal)?

3. Methodologies

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Problem Posing

Problem Solving

Learning by doing

Collaborative learning

Automatic Formative Assessment

.....

4. Type of activities and timing

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Specify in detail the various components of the activity

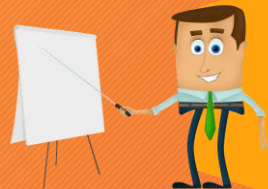


Individual activities

Group activities



Theoretical presentations



Time scan for each of the various phases into which the activity is divided



5. Technologies

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Specific software

- Geogebra, Maple, Autocad....

Tools to increase participation

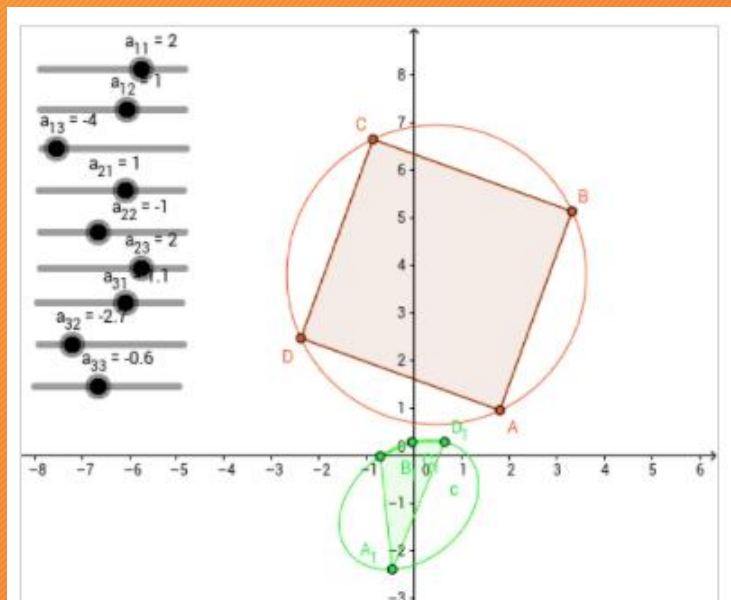
- Mentimeter, google form, Wooclap ...

Better if all integrated into a DLE

- For example, Moodle integrated with other software: activities such as the questionnaire, the forum, the delivery, the quiz, the workshop and multiple resources

6. Poor materials and interactive materials

- Paper, pen, scissors,....
- Open educational resources: videos, images, ...
- Interactive materials prepared ad hoc



Projection of a Vector onto a Plane

Main Concept

Recall that the vector projection of a vector \vec{u} onto another vector \vec{v} is given by $proj_{\vec{v}}(\vec{u}) = \frac{\vec{u} \cdot \vec{v}}{\|\vec{v}\|^2} \vec{v}$.

The **projection of \vec{u} onto a plane** can be calculated by subtracting the component of \vec{u} that is orthogonal to the plane from \vec{u} . If you think of the plane as being horizontal, this means computing \vec{u} minus the vertical component of \vec{u} , leaving the horizontal component. This "vertical" component is calculated as the projection of \vec{u} onto the plane normal vector \vec{n} .

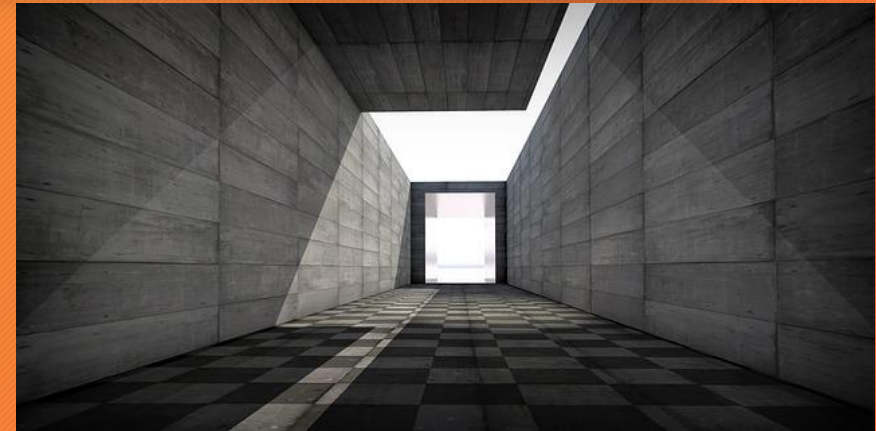
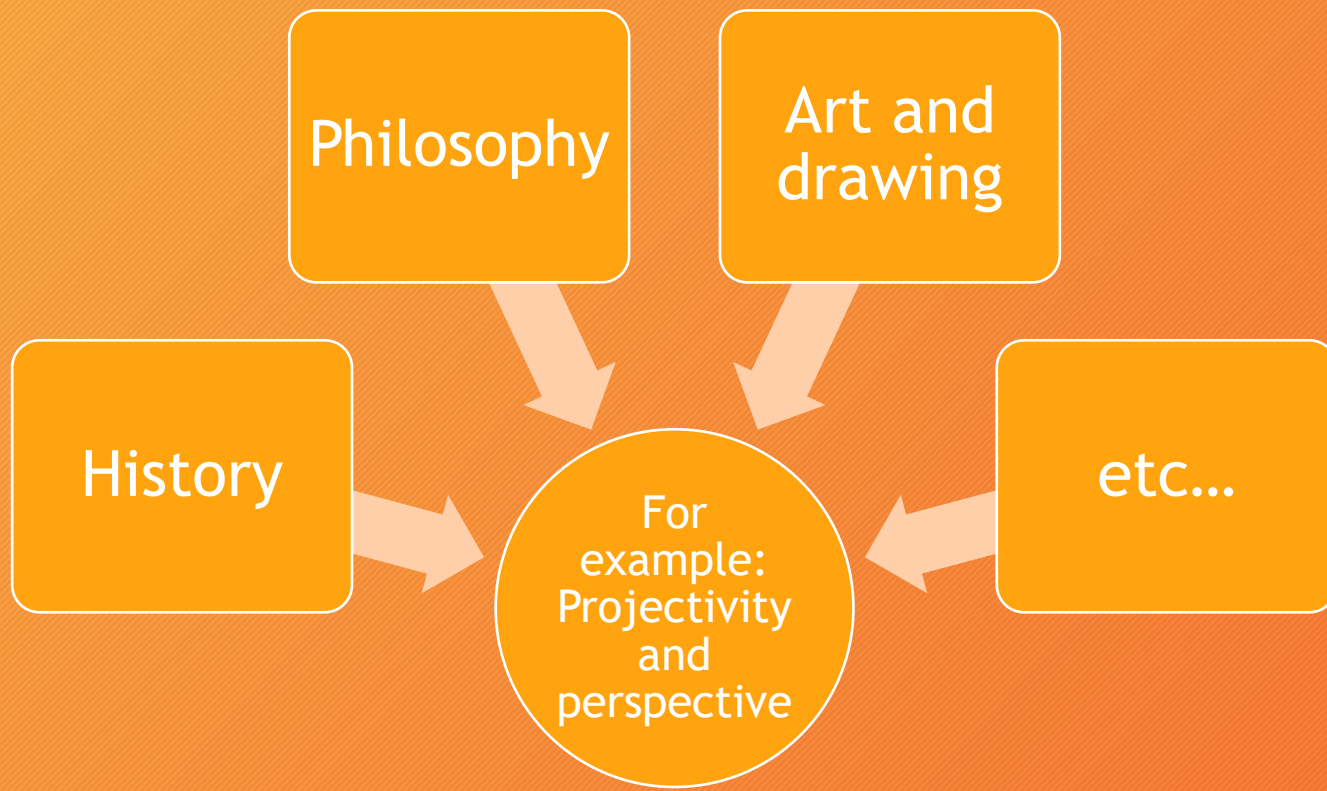
$$proj_{Plane}(\vec{u}) = \vec{u} - proj_{\vec{n}}(\vec{u}) = \vec{u} - \frac{\vec{u} \cdot \vec{n}}{\|\vec{n}\|^2} \vec{n}$$

Choose the coordinates of a plane normal vector \vec{n} and a vector \vec{u} and notice how the perpendicular of the vector projection of \vec{u} onto \vec{n} is the projection of \vec{u} onto the plane.

Normal Vector \vec{n}			Vector \vec{u}		
$x_n =$	<input type="text" value="-10.0"/>	<input type="text" value="0.0"/>	$x_u =$	<input type="text" value="-10.0"/>	<input type="text" value="0.0"/>
$y_n =$	<input type="text" value="-10.0"/>	<input type="text" value="0.0"/>	$y_u =$	<input type="text" value="-10.0"/>	<input type="text" value="0.0"/>
$z_n =$	<input type="text" value="-10.0"/>	<input type="text" value="0.0"/>	$z_u =$	<input type="text" value="-10.0"/>	<input type="text" value="0.0"/>
<input type="checkbox"/> Projection of u onto n			<input type="checkbox"/> Projection of u onto the plane		

7. Multi- and interdisciplinary

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Città ideale - Galleria Nazionale delle Marche, Palazzo Ducale di Urbino
<http://www.gallerianazionalemarche.it/collezioni-gnm/citta-ideale/>

8. Inclusion

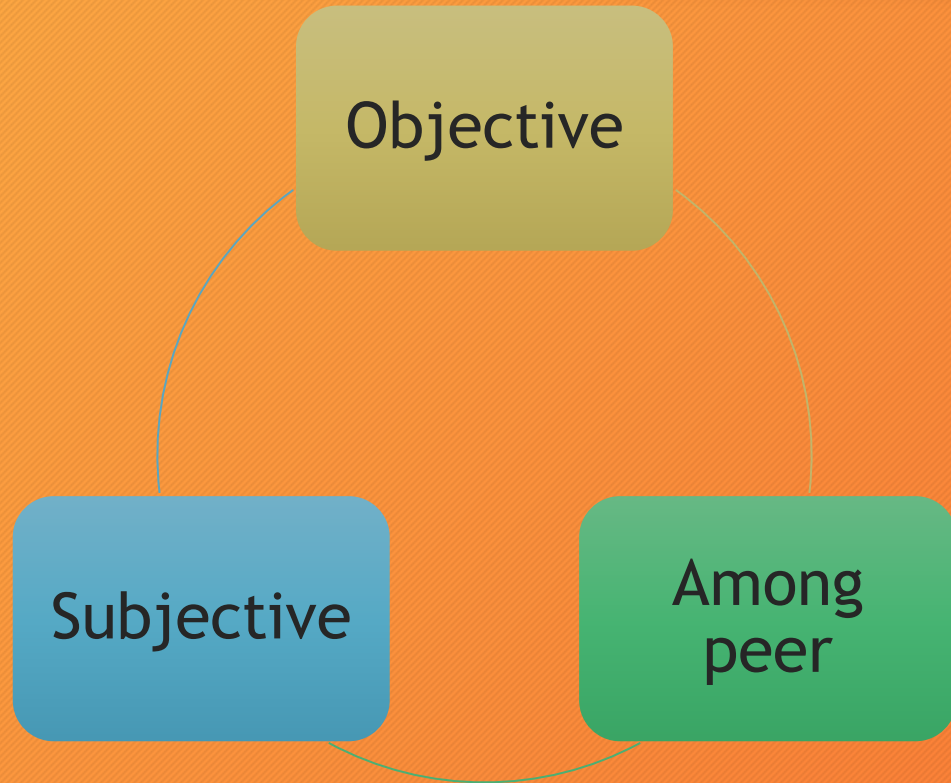
65

It means taking into account special educational needs (for example, visually impaired, dyslexic, ...) and then setting the teaching activity in a way that can be personalized, adapted (adaptive teaching and learning)

It can be done in different ways: by planning different activities, using specific fonts, making materials available....

9. Evaluation

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 For each it is important to clarify and share an assessment grid and learning objectives

What kind of evaluation?

- among peers
- objective
- subjective

What kind of feedback can I give through this activity?

- general feedback
- interactive feedback

Subjective evaluation

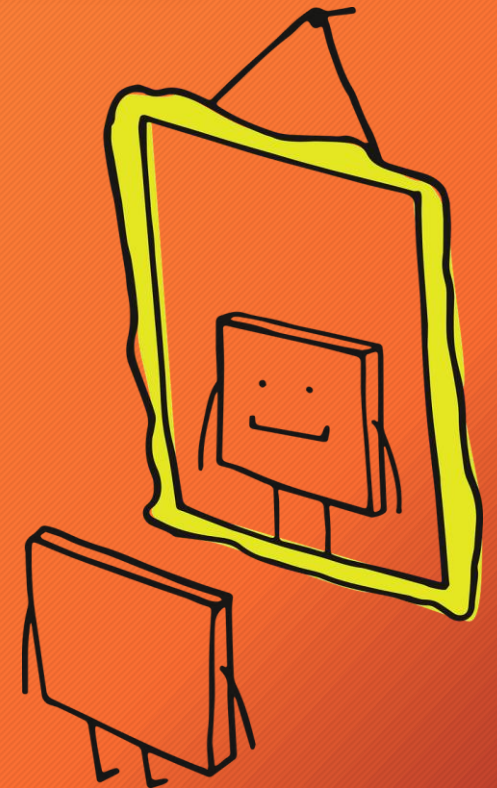
67

Through self-assessment and reflection, students learn to evaluate their learning and reflect on their work



It is important that the student:

- Understand the learning objectives
- Understand how the business is valued
- Get feedback
- Have the opportunity to confront a good practice



Peer evaluation

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Each student evaluates the work of their peers based on the same grid of evaluation that they would have used to evaluate their own

Delivery phase of an assignment

- From every student
- In a certain time frame



Destruction of one or more deliveries to each student

- Manual or automatic
- Different from their own



Evaluation phase

- With a well-defined evaluation grid
- Possibility to insert comments
- In a certain time frame



Publication of evaluations

- Each student can take one grade for submission and one grade for assessment

Objective evaluation

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Diagnostic evaluation

- To detect the adequacy of students' preparation in relation to the planning of new teaching activities

Formative evaluation

- To detect pupils' learning in progress and how they receive new knowledge

Summative evaluation

- To detect the knowledge and skills at the end of the learning units

10. Metariflexion

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Do the materials meet the needs of the students?

At what point of the activity can my students encounter problems or difficulties?

Are feedback and suggestions helpful in overcoming these difficulties?

Does the evaluation take into account all aspects of the activity?

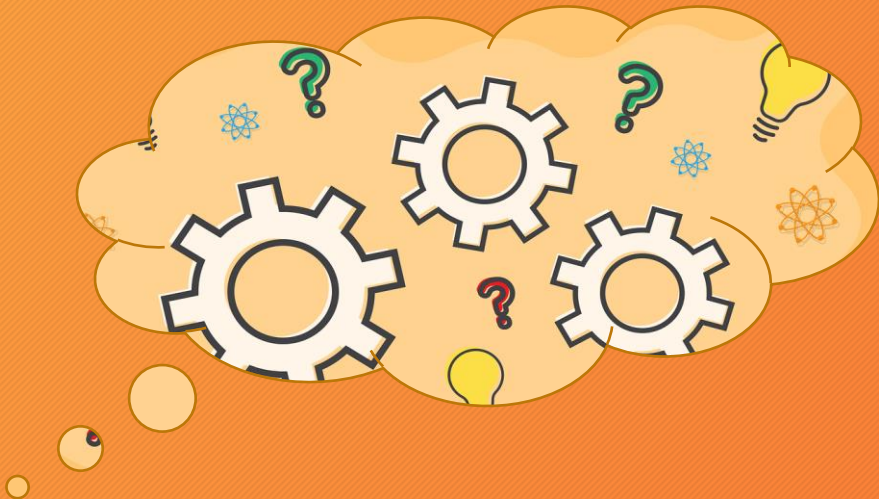
Are the objectives and prerequisites consistent with the activity?

What difficulties did I encounter in planning the activity?

Activity: first steps for planning an educational activity

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Now it's your turn! Design an educational activity of your choice.



Objectives / Prerequisites

Topic

Class

Type of institution

Period

- Context
- Didactic objectives
- Prerequisites
- Estimated time

Methodologies

Type of activities and timing

Technologies and materials

References (1/2)

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Thank you for the attention!

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